

ADVANCED SUBSIDIARY GCE MATHEMATICS

4728

Mechanics 1

Candidates answer on the Answer Booklet

OCR Supplied Materials:

- 8 page Answer Booklet
- List of Formulae (MF1)

Other Materials Required:

None

Monday 19 January 2009 Afternoon

Duration: 1 hour 30 minutes



INSTRUCTIONS TO CANDIDATES

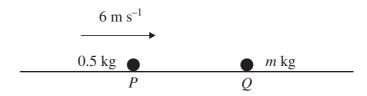
- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- Do **not** write in the bar codes.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- The acceleration due to gravity is denoted by $g \, \mathrm{m \, s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use g = 9.8.
- You are permitted to use a graphical calculator in this paper.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is **72**.
- This document consists of 4 pages. Any blank pages are indicated.

2

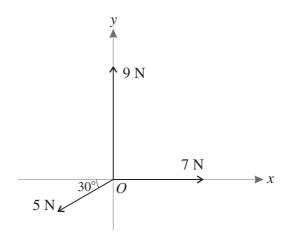
1



A particle P of mass 0.5 kg is travelling with speed $6 \,\mathrm{m\,s^{-1}}$ on a smooth horizontal plane towards a stationary particle Q of mass $m \,\mathrm{kg}$ (see diagram). The particles collide, and immediately after the collision P has speed $0.8 \,\mathrm{m\,s^{-1}}$ and Q has speed $4 \,\mathrm{m\,s^{-1}}$.

- (i) Given that both particles are moving in the same direction after the collision, calculate m. [3]
- (ii) Given instead that the particles are moving in opposite directions after the collision, calculate m.
- A trailer of mass 500 kg is attached to a car of mass 1250 kg by a light rigid horizontal tow-bar. The car and trailer are travelling along a horizontal straight road. The resistance to motion of the trailer is 400 N and the resistance to motion of the car is 900 N. Find both the tension in the tow-bar and the driving force of the car in each of the following cases.
 - (i) The car and trailer are travelling at constant speed. [3]
 - (ii) The car and trailer have acceleration $0.6 \,\mathrm{m \, s^{-2}}$.

3

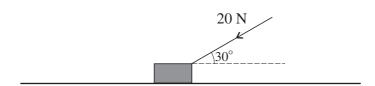


Three horizontal forces act at the point O. One force has magnitude 7 N and acts along the positive x-axis. The second force has magnitude 9 N and acts along the positive y-axis. The third force has magnitude 5 N and acts at an angle of 30° below the negative x-axis (see diagram).

- (i) Find the magnitudes of the components of the 5 N force along the two axes. [2]
- (ii) Calculate the magnitude of the resultant of the three forces. Calculate also the angle the resultant makes with the positive *x*-axis. [6]

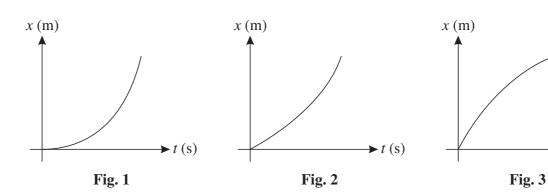
3

4



A block of mass 3 kg is placed on a horizontal surface. A force of magnitude 20 N acts downwards on the block at an angle of 30° to the horizontal (see diagram).

- (i) Given that the surface is smooth, calculate the acceleration of the block. [3]
- (ii) Given instead that the block is in limiting equilibrium, calculate the coefficient of friction between the block and the surface. [5]
- 5 A car is travelling at $13 \,\mathrm{m\,s^{-1}}$ along a straight road when it passes a point *A* at time t = 0, where *t* is in seconds. For $0 \le t \le 6$, the car accelerates at $0.8t \,\mathrm{m\,s^{-2}}$.
 - (i) Calculate the speed of the car when t = 6. [5]
 - (ii) Calculate the displacement of the car from A when t = 6. [5]
 - (iii) Three (t, x) graphs are shown below, for $0 \le t \le 6$.



- (a) State which of these three graphs is most appropriate to represent the motion of the car. [1]
- (b) For each of the two other graphs give a reason why it is not appropriate to represent the motion of the car. [2]

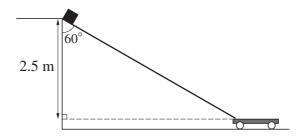
[Questions 6 and 7 are printed overleaf.]

 $\rightarrow t$ (s)

4

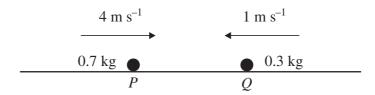
- 6 Small parcels are being loaded onto a trolley. Initially the parcels are 2.5 m above the trolley.
 - (i) A parcel is released from rest and falls vertically onto the trolley. Calculate
 - (a) the time taken for a parcel to fall onto the trolley, [2]
 - (b) the speed of a parcel when it strikes the trolley. [2]

(ii)



Parcels are often damaged when loaded in the way described, so a ramp is constructed down which parcels can slide onto the trolley. The ramp makes an angle of 60° to the vertical, and the coefficient of friction between the ramp and a parcel is 0.2. A parcel of mass 2 kg is released from rest at the top of the ramp (see diagram). Calculate the speed of the parcel after sliding down the ramp.

7



Two particles P and Q have masses 0.7 kg and 0.3 kg respectively. P and Q are simultaneously projected towards each other in the same straight line on a horizontal surface with initial speeds of $4 \,\mathrm{m\,s^{-1}}$ and $1 \,\mathrm{m\,s^{-1}}$ respectively (see diagram). Before P and Q collide the only horizontal force acting on each particle is friction and each particle decelerates at $0.4 \,\mathrm{m\,s^{-2}}$. The particles coalesce when they collide.

- (i) Given that P and Q collide 2 s after projection, calculate the speed of each particle immediately before the collision, and the speed of the combined particle immediately after the collision. [6]
- (ii) Given instead that P and Q collide 3 s after projection,
 - (a) sketch on a single diagram the (t, v) graphs for the two particles in the interval $0 \le t < 3$, [3]
 - (b) calculate the distance between the two particles at the instant when they are projected. [6]



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